# Fiscal Multipliers in Small Open Economies With Heterogeneous Households\*

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#### **Abstract**

We study fiscal multipliers in a small open economy Heterogeneous Agent New Keynesian (SOE-HANK) model. We provide a set of equivalence results under which the fiscal multiplier in our SOE-HANK model is the same—at any horizon—as in a corresponding representative-agent (RANK) model. Under more general assumptions, the fiscal multipliers in the two models are not equivalent, but remain relatively similar. Yet, we show that the underlying channels driving the fiscal multipliers differ substantially. In particular, consumption increases while net exports tend to decline in the HANK model, whereas the opposite is true in the RANK model.

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# **1 Introduction**

In this paper, we study fiscal multipliers in the context of a small open economy model with nominal rigidities, incomplete financial markets, and heterogeneous households, i.e., a SOE-HANK model. Previous literature has established that, in a closed-economy setting, fiscal multipliers are in general substantially higher when financial markets are incomplete and a fraction of households have limited access to credit markets, as compared to the case of a standard complete-markets model with a representative agent (RANK); see, e.g., Galí et al. (2007), Hagedorn et al. (2019), Bilbiie (2020), or Auclert et al. (2023). In a nutshell, the presence of a considerable fraction of households with (realistically) high marginal propensities to consume (MPCs) generates a "Keynesian multiplier effect" on aggregate demand. In an open economy, there are two reasons why this logic may not hold up, or at least have a smaller quantitative impact: *First*, the Keynesian multiplier exerts a weaker effect on aggregate domestic demand, since a portion of the additional income will be spent on imported goods. *Second*, to the extent that aggregate domestic demand increases, this will tend to appreciate the real exchange rate, thereby reducing net exports. On the other hand, any appreciation raises the real purchasing power of domestic households and thus works in the opposite direction (the "real income channel" discussed by Auclert et al., 2021b). Against this backdrop, our aim is to compare fiscal multipliers in the SOE-HANK model to those obtained in a corresponding RANK model.

We start by decomposing the output response into six distinct channels in stylized versions of the models. The first four of these channels are also present in a closedeconomy setting, while the last two only operate in an open economy. The output response to a change in government spending is composed of (i) the direct effect of the spending increase, (ii) the effect from higher tax burdens on spending, (iii) intertemporal substitution effects via interest rate changes, (iv) a Keynesian multiplier effect, (v) expenditure switching effects from changes in the real exchange rate, and (vi) real income effects from changes in the real exchange rate. The relative magnitudes of these are not unambiguous. The drag from taxes tends to be larger in HANK, the drag from intertemporal substitution larger in RANK; Keynesian multiplier and real income effects tend to boost the multiplier in HANK compared to RANK, while the relative effect of expenditure switching is unclear a priori.

Guided by the decomposition, we then show that, under some restrictions on parameters, the multipliers in the two frameworks are equivalent. First, we show that, in the limiting case of complete openness, the fiscal multiplier in HANK and RANK is

identical. Complete openness implies that the home consumption basket contains only foreign goods. As a result, household income does not affect spending on domestically produced goods, so the Keynesian multiplier is shut down, and the financing and intertemporal substitution channels have no effect on domestic output. If the real interest rate and thus the real exchange rate stay constant, output rises by exactly the size of the fiscal stimulus. If the real interest rises to stabilize output, then the real exchange rate appreciates and expenditure switching exactly crowds out the fiscal stimulus (reminiscent of the standard Mundell–Fleming result).

Second, a comparable but slightly less general equivalence result obtains when we consider the degree of substitutability between foreign and domestic goods. In the limiting case of infinite substitutability, we can show that fiscal multipliers coincide in HANK and RANK, and equal zero provided monetary policy is active. Fiscal spending is fully crowded out in this case via taxes in the HANK model and expenditure switching in both models, as the real rate rises and the real exchange rate appreciates.

Third, if the elasticity is unity and the fiscal stimulus is financed with a balancedbudget increase in taxes, we can show that the multipliers in both models are identical at all horizons and non-negative. In this case, income and substitution effects from real exchange rate changes offset each other so net exports are unchanged, and the economy behaves almost as a closed economy.

We then show numerically that for every value of the trade elasticity, there is a degree of financing that equalizes the multipliers across models (or vice versa). The multiplier in HANK is larger compared to RANK the less of the stimulus is financed with taxes, and the smaller the trade elasticity. A lower trade elasticity makes expenditure switching weaker which raises multipliers in both models. It does so more in HANK than RANK because of the additional Keynesian multiplier effect.

Overall, our results highlight that, in an open economy, the effectiveness of fiscal spending depends not just on MPCs, but importantly on openness, trade elasticities, and their interaction with financing of the stimulus. It is not clear, in particular, that an open economy HANK framework features higher multipliers than the corresponding RANK model: If enough of the stimulus is financed with taxes, or if preferences are such that a substantial part of the stimulus is spent abroad, then these effects can dominate higher marginal propensities to consume and lead to smaller multipliers in HANK compared to RANK.

We proceed to compare fiscal multipliers in quantitative versions of the models. The stylized HANK model was parameterized to replicate empirically observed MPCs since that is central to our question of fiscal multipliers. In the quantitative model, we also incorporate a standard monetary policy reaction function, debt stationarity, and introduce a number of standard features that allow us to match additional relevant moments (debt levels, wealth levels and markups, time-varying trade elasticities). In these quantitative models, we show that multipliers across HANK and RANK are similar. The impact multiplier is 1.11 in the HANK model and 0.93 in the RANK model. This difference is smaller than what is typically found in the closed-economy literature, see, e.g., Auclert et al. (2023). Furthermore, present-value multipliers are relatively small in our setting since output displays comparatively little persistence in both models.

Even though multipliers are of a similar magnitude, the underlying dynamics is quite different across the two models. In the HANK model, a fiscal expansion is accompanied by a consumption boom which is partly offset by a drop in net exports. The overall result is a multiplier that is comparable to the RANK model, where consumption falls and net exports rise.

We show in a number of sensitivity exercises that this conclusion does not substantially change with the responsiveness of monetary policy or realistic variations in the level of the trade elasticity. The reason is that neither breaks the positive comovement between consumption and imports in HANK relative to RANK. Quantitatively, a similar argument applies when altering the degree of debt financing, which therefore turns out to be less important in the open economy than in a closed-economy setting. Openness and the nature of nominal rigidities are somewhat more important in driving the gap in fiscal multipliers between HANK and RANK models. More open economies are characterized by a larger leakage of demand; whereas a model with sticky prices and flexible wages weakens the negative comovement between consumption and net exports observed in most other cases. Finally, the similarity of HANK and RANK multipliers is robust to a range of additional modifications of our baseline model environment, including the introduction of capital, a fixed nominal exchange rate, and alternative paths of the real exchange rate.

# **1.1 Related Literature**

Our paper contributes to a large literature on fiscal multipliers, see Ramey (2019) for a recent survey. In a closed economy, Keynesian theories predict large output effects from increased government spending due to Keynesian multiplier effects. Neoclassical models on the other hand emphasize downward pressure on private

consumption due to negative wealth effects from higher (future) taxation, and thus tend to predict small multipliers, as for example in Baxter and King (1993). New Keynesian models with representative agents can generate sizeable fiscal multipliers, with the magnitude depending on the source and extent of nominal rigidities, as well as the response of monetary policy, see for example Woodford (2011). In open economies, Erceg and Linde (2012), Corsetti et al. (2013), and Nakamura and Steinsson (2014) show that fiscal multipliers are generally low in flexible exchange-rate open economies, which is consistent with the traditional Mundell–Fleming view that fiscal policy is more effective in fixed exchange-rate regimes.

More recently, studies of fiscal spending have turned to the empirically realistic case of heterogeneous agents. In a closed-economy setting, fiscal multipliers are found to be substantially higher under incomplete financial markets, as compared to the case of a standard complete-markets model with a representative agent; see, e.g., Galí et al. (2007), Bilbiie (2020), Hagedorn et al. (2019) or Auclert et al. (2023).<sup>1</sup>

A number of recent papers have extended the HANK framework to an international setting, including De Ferra et al. (2020), Auclert et al. (2021b), Bellifemine et al. (2023), Guo et al. (2023), Oskolkov (2023), and Bayer et al. (2024). In our own previous work, we contribute to—and offer a short survey of—this emerging strand of the literature; see Druedahl et al. (2022). To the best of our knowledge, fiscal multipliers have not previously been systematically studied in this framework.

Our contribution in this paper is to quantify the relationship between fiscal multipliers in open-economy HANK versus open-economy RANK models. In closed economies, the literature has shown that allowing for heterogeneous agents magnifies estimates of fiscal multipliers; we ask whether this remains true when instead looking at an open economy. Our results indicate that multipliers tend to be similar in open economies across HANK and RANK frameworks, and can indeed be identical, but that the implied dynamics is quite different. In particular, in the HANK model multipliers work via a consumption boom and a trade deficit, whereas it is the reverse in the RANK setting.

These results are consistent with Farhi and Werning (2016) who study, among other things, fiscal policy in open economies with hand-to-mouth agents. They show that

<sup>1.</sup> In this respect, the study by Broer et al. (2023) represents a notable exception, as they present several cases in which the HANK and RANK multipliers coincide. Their model differs from most of the HANK literature, since only "capitalists"—who receive profits, but no labor income—display a high MPC, thus effectively shutting down the intertemporal Keynesian labor-income multiplier.

trade deficits emerge and that therefore fiscal stabilization is more effective when regions are less open to trade. Aggarwal et al. (2023) study fiscal transfers in a multicountry HANK setting and show likewise that these lead to persistent trade deficits.

Our results also speak to the empirical debate on the effects of fiscal policy on open economy variables such as the real exchange rate and the trade balance. Existing empirical studies have found evidence of an increase in private consumption along with a worsening of the trade balance in response to a fiscal expansion, in line with the implications of our HANK model, see, e.g., Corsetti and Müller (2006), Monacelli and Perotti (2010), and Ravn et al. (2012). Lambertini and Proebsting (2023) find that fiscal policy primarily affects imports rather than exports both in terms of prices and quantities, and that real exchange rate responses are driven by relative changes in the price of nontraded goods instead (a fiscal expansion raises the relative price of services, not exports). This is consistent with our theoretical results.

### **1.2 Structure**

We start by presenting a stylized model in Section 2. We use this model to derive and discuss analytical results about fiscal multipliers in Section 3. In Section 4, we provide numerical results on fiscal multipliers in a larger model. Section 5 concludes.

# **2 A Stylized Model of Fiscal Multipliers**

In this section, we study fiscal policy in a small open economy (SOE) with a general household problem. The core of the model is similar to the one considered by Auclert et al. (2021b)—which in turn is an incomplete-markets version of the canonical SOE model of Galí and Monacelli (2005)—extended with fiscal policy. We keep the model simple in order to highlight some special cases where the fiscal multipliers obtained in the HANK and RANK models coincide. Studying these cases helps us understand the channels at work in each of the two models.

# **2.1 Model Description**

We consider the sequence-space representation of the model following Auclert et al. (2021a). In this framework, the key objects are the infinite-dimensional vectors

of perturbations of variables from steady state,  $dX = (dX_0, dX_1, ...)$ , where  $dX_t \approx$  $X_t - X_{ss}$  is the deviation from steady state for any variable *X*. We restrict our attention to perfect-foresight shocks.

#### **2.1.1 Households**

We consider two household structures. The first case is a heterogeneous-agents (HA) model featuring a continuum of households. A household with assets *at*−<sup>1</sup> and idiosyncratic earnings  $e_t$  chooses consumption  $c_t$  and end-of-period assets  $a_t$  to solve

$$
V_t(a_{t-1}, e_t) = \max_{c_t, a_t} \log c_t + \beta \mathbb{E}_t \left[ V_{t+1}(a_t, e_{t+1}) \right],
$$
  
s.t.  

$$
c_t + a_t = (1 + r_t^a) a_{t-1} + Z_t e_t,
$$

$$
a_t \ge 0,
$$
  

$$
\ln e_t = \rho_e \ln e_{t-1} + \epsilon_t^e, \quad \epsilon_t^e \sim \mathcal{N}\left(0, \sigma_e^2\right),
$$

where  $r_t^a$  denotes real asset returns.  $Z_t = (1 - \tau_t)w_tN_t$  is real labor income, where  $w_t$ is the real wage rate,  $N_t$  is labor supply, and  $\tau_t$  is the tax rate. Idiosyncratic income, *et* , follows an AR(1) process in logs with i.i.d. normal innovations. The household has access to three types of assets: domestic government bonds (which pay the real interest rate *rt*), foreign bonds (which pay a fixed real rate *r* ∗ ), and domestic equity (which pays real after-tax dividends *Dt*). With perfect international capital mobility, this gives rise to the following two no-arbitrage conditions:

$$
1 + r_t = \frac{D_{t+1} + p_{t+1}^D}{p_t^D},\tag{1}
$$

$$
1 + r_t = (1 + r^*) \frac{Q_{t+1}}{Q_t}, \tag{2}
$$

where  $r_t = \mathbb{E}_t r_t^a$  $t_{t+1}^a$  is the ex-ante real return, and  $p_t^D$  is the price of firm equity.<sup>2</sup>  $Q_t \equiv E_t \frac{P^*}{P_t}$  $\frac{P^*}{P_t}$  is the real exchange rate, with  $E_t$  denoting the nominal exchange rate (the price of foreign currency in terms of domestic currency), and where we normalize

<sup>2.</sup> Along the perfect foresight transition path, the ex-post and ex-ante returns are equalized;  $r_t^a = r_{t-1}$ for  $t = 1, 2, \ldots$  . Ex-post returns in period zero are given by  $r_0^a = \frac{p_0^D + D_0}{p_{\infty}^D}$  $\frac{+D_0}{p_{ss}^D}$ , since we assume that both foreign and domestic bond holdings are zero in steady state, i.e.,  $B_{ss} = B_{ss}^* = 0$ .

 $P^* = 1$ . It then follows that (1) equates the real return on domestic stocks and bonds, while (2) is a real UIP condition, stating that the expected real return on foreign and domestic assets must be equalized.

As an alternative to the HA structure, we also consider a standard representativeagent (RA) model, where the household acts according to a standard Euler equation for all  $t = 0, 1, ...$ :

$$
C_t^{-1} = \beta (1 + r_{t+1}^a) C_{t+1}^{-1},
$$

with  $C_{\infty} = C_{ss}$ . This version of the model is similar to the one considered by Galí and Monacelli (2005), with the exception that we do not allow for international risk sharing, whereas their setup features perfect risk sharing across countries.

For a given level of domestic consumption, *C<sup>t</sup>* , domestic households split consumption between home and foreign goods with home bias  $(1 - \alpha) \in (0, 1)$  as follows:

$$
C_{H,t} = (1 - \alpha) \left(\frac{P_{H,t}}{P_t}\right)^{-\eta} C_t, \text{ and } C_{F,t} = \alpha \left(\frac{P_{F,t}}{P_t}\right)^{-\eta} C_t,
$$
 (3)

where *CH*,*<sup>t</sup>* and *CF*,*<sup>t</sup>* denote domestic consumption of domestic and foreign goods, respectively, and  $P_{H,t}$  and  $P_{F,t}$  are the prices of these.  $\eta$  is the elasticity of substitution between domestic and foreign goods, and *P<sup>t</sup>* is the consumer price index (CPI),

$$
P_t = \left[ (1 - \alpha) P_{H,t}^{1 - \eta} + \alpha P_{F,t}^{1 - \eta} \right]^{\frac{1}{1 - \eta}}.
$$
 (4)

#### **2.1.2 Firms**

Production is linear in labor,  $Y_t = N_t$ . The price of home goods in domestic currency is set as a markup over the nominal wage,  $P_{H,t} = \mu W_t$ , where  $W_t = w_t P_t$ . The price in foreign currency is then pinned down through the nominal exchange rate, *E<sup>t</sup>* , and the law of one price:

$$
P_{H,t}^* = \frac{P_{H,t}}{E_t}.\tag{5}
$$

Real dividends net of taxes are:

$$
D_t = (1 - \tau_t) \frac{P_{H,t} Y_t - W_t N_t}{P_t}.
$$
\n(6)

The source of nominal rigidities in our model is sticky wages, implying a standard new-Keynesian wage Phillips curve (NKWPC), following Auclert et al. (2021b):

$$
\pi_{W,t} = \kappa \left( \frac{\psi N_t^{\varphi}}{(1 - \tau_t) w_t U_{c_t} / \mu} - 1 \right) + \beta \pi_{W,t+1}, \tag{7}
$$

where  $\pi_{W,t} \equiv W_t/W_{t-1}-1$  is nominal wage growth and  $U'_{c_t}$  denotes productivityweighted aggregate marginal utility of consumption.<sup>3</sup> This is consistent with a micro-foundation where a union sets nominal wages to maximize average household welfare, given the same labor supply *N<sup>t</sup>* for all households.

#### **2.1.3 Government**

The government has a standard budget constraint:

$$
B_t = (1 + r_{t-1})B_{t-1} + \frac{P_{H,t}}{P_t}G_t - T_t,
$$
\n(8)

where real tax receipts are given by:

$$
T_t = \tau_t \left( w_t N_t + \frac{P_{H,t} Y_t - W_t N_t}{P_t} \right) = \tau_t \frac{P_{H,t}}{P_t} Y_t.
$$

We assume that government consumption, *G<sup>t</sup>* , displays a home bias of 1. Furthermore,  $G_t$  is assumed to be exogenous, following an AR(1) process with persistence  $\rho_G.$  The tax rate, *τ<sup>t</sup>* , adjusts to ensure that tax receipts satisfy

$$
T_t - T_{ss} = \phi_G (G_t - G_{ss}). \tag{9}
$$

For analytical simplicity, we restrict our attention to a steady state characterized by a balanced government budget and no government debt; *Bss* = 0. Additionally, the steady state we consider is in the vicinity of  $r_{ss} = 0$ , so that the steady-state version of (8) implies  $G_{ss} = T_{ss}$ . We proceed by setting both of these to zero, but slightly modified versions of the equivalence results presented below hold for any level of tax revenues and government spending satisfying  $G_{ss} = T_{ss}$ . We relax these assumptions when we turn to numerical analyses in Section 4. As for monetary policy, we assume

<sup>3.</sup> In HANK this is given by  $U'_{c_t} = \int e_t c_t (a_{t-1}, e_t) d_t(a_{t-1}, e_t)$  where  $t_i$  is the distribution of households over states. In RANK it is simply  $U'_{c_t} = C_t^{-1}$ .

that it is governed by the following real interest-rate rule:

$$
r_t = r_{ss} + \phi_Y \left(\frac{Y_t}{Y_{ss}} - 1\right),\tag{10}
$$

with  $\phi_Y \geq 0$ . The absence of a monetary policy response to inflation simplifies the analytical solution of the model, as it implies that the Phillips curve (7) does not enter in the determination of real variables (though it matters for nominal variables). However, given that the responses of output and inflation to a government spending shock usually have the same sign in our model, this choice is not crucial from a qualitative viewpoint. We consider a more general interest-rate rule in Section 4.

#### **2.1.4 The Foreign Economy**

The consumption of domestically produced goods by foreign consumers is given by:

$$
C_{H,t}^* = \alpha \left( P_{H,t}^* \right)^{-\eta} C_{ss}^*,
$$
\n(11)

with  $C_{ss}^* = C_{ss}$  denoting the fixed level of foreign consumption. With  $P^* = 1$ , the law of one price implies that  $E_t = P_{F,t}$ .

#### **2.1.5 Goods Market Clearing**

Lastly, goods market clearing for tradable goods is:

$$
Y_t = C_{H,t} + C_{H,t}^* + G_t.
$$
 (12)

Defining net exports as  $NX_t = \frac{P_{H,t}}{P_t}$  $\frac{P_{H,t}}{P_t} C_{H,t}^* - \frac{P_{F,t}}{P_t}$  $\frac{F_t}{P_t}C_{F,t}$ , the above expression can also be expressed as  $\frac{P_{H,t}}{P_t}Y_t = C_t + \frac{P_{H,t}}{P_t}$  $\frac{H_t}{P_t}G_t + N X_t$ .

## **2.2 Equilibrium and Solution**

We define the overall equilibrium of model as:

**Definition 1** (Equilibrium)**.** *Given sequences for G<sup>t</sup> and T<sup>t</sup> , an initial household distribution over assets and earnings*  $\mathcal{D}_0(a,e)$ , and an initial portfolio allocation between foreign and *domestic assets, a competitive equilibrium in the domestic economy is a path of household* *policies*  $\{c_t(a_{t-1}, e_t), a_t(a_{t-1}, e_t)\}$ , distributions  $\mathcal{D}_t(a, e)$ , prices:

$$
\{E_t, Q_t, P_t, P_{H,t}, P_{F,t}, W_t, p_t^D, r_t, r_t^a\},\
$$

*and quantities:*

$$
\{C_t, C_{H,t}, C_{F,t}, Y_t, N_t, D_t, \tau_t, B_t\},\
$$

*such that all households and firms optimize, monetary and fiscal policy follow their rules, and the goods market* (12) *clears.*

In the numerical solution of the model we solve the households' problem using the endogenous grid method of Carroll (2006). We then rely on the "fake news algorithm" of Auclert et al. (2021a) to compute the Jacobian of the household problem around the deterministic steady state. The full non-linear transition paths are solved for using Broyden's method.<sup>4</sup>

# **3 The Fiscal Multiplier in HANK and RANK**

Building on the model established above, we now characterize the fiscal multiplier under each of the two household structures: The HANK and the RANK model.

# **3.1 The Output Response to a Fiscal Policy Shock**

Consider the equilibrium following a fiscal policy shock, i.e. paths of government consumption,  $(G_t)_{t=0}^{\infty}$ , and taxes,  $(T_t)_{t=0}^{\infty}$ .

**Proposition 1.** An equilibrium of the model with household structure  $j \in \{RA, HA\}$ *following a fiscal policy shock satisfies*

$$
dY^{j} = \underbrace{dG}_{1. \text{ Gov. consumption}} - \underbrace{(1-\alpha)M^{j}dT}_{2. \text{ Taxes}} + \underbrace{(1-\alpha)R^{j}dr^{j}}_{3. \text{ Interest rate}} + \underbrace{(1-\alpha)M^{j}dY^{j}}_{4. \text{ Multiplier}} + \underbrace{\frac{2-\alpha}{1-\alpha}\alpha\eta dQ^{j}}_{5. \text{ Exp. switching}} - \underbrace{\alpha M^{j}dQ^{j}}_{6. \text{ Real income}} ,
$$

<sup>4.</sup> The code is written in Python and based on the GEModelTools package.

*where M<sup>j</sup> is the matrix of intertemporal marginal propensities to consume, and R j is the matrix of intertemporal effects on consumption of real interest rate changes.*

*Proof.* See Appendix A.1.

Proposition 1 decomposes the response of output across different models into six channels. Conceptually, the first four of these channels are also operative in a closed economy, while the last two only appear in an open economy. We now consider each of the channels separately, and discuss how they differ across models. While Proposition 1 holds for any set of paths  $(G_t, T_t)_{t=0}^{\infty}$  and any monetary policy rule, we now consider an increase in government consumption, *dG<sup>t</sup>* > 0 partly financed by higher taxes,  $dT_t \geq 0$ , with monetary policy following the rule given by (10).

- 1. **Government consumption.** Higher government consumption increases output directly via goods market equilibrium. This channel is independent of household behavior, and thus equivalent in the two models.
- 2. **Taxes.** Higher taxes reduce spending. The strength of this channel depends on the MPC, which is governed by household behavior. In the RANK model the MPC is low, so this channel is weak. In the HANK model the MPC is higher, so the channel is potentially strong.

Note that, in an open economy, this channel as well as the next two are scaled by the factor  $(1 - \alpha)$ , reflecting the fact that only a fraction  $(1 - \alpha)$  of income is spent at home, with the rest flowing abroad.

- 3. **Interest rate.** The real interest rate is likely to change in response to fiscal policy. If the real interest rate increases—which will typically be the case given the interest rate rule we have assumed—households increase savings and reduce current consumption (intertemporal substitution). This channel is likely to be stronger in the RANK model than in the HANK model (see Kaplan et al., 2018 or Druedahl et al., 2022).
- 4. **Multiplier.** Higher output means more labor income, which in turn implies higher consumption, and thus higher output. This is the intertemporal Keynesian multiplier (Auclert et al., 2023).
- 5. **Expenditure switching.** Given a positive response of the domestic real interest rate, the real exchange rate appreciates through the UIP (i.e.,  $dQ_t <$

 $0$ .<sup>5</sup> This makes domestic goods more expensive, inducing both domestic and foreign consumers to substitute away from them, reducing output. This channel depends on the magnitude of the appreciation, which can differ across models depending on household behavior, as well as the trade elasticity, *η*.

6. **Real income.** As the real exchange rate appreciates, this stimulates the real purchasing power of domestic households, who then consume more, boosting output. How much spending is increased depends on the MPC, so this channel is stronger in the HANK model than in the RANK model, as argued by Auclert et al. (2021b).

In Table 1, we summarize the signs of the channels in the two models. This table is helpful in order to determine which of the two models displays the largest fiscal multiplier, and how this may be affected when going from a closed to an open economy.

First, the combination of channels 2, 3, and 4 tend to imply a larger fiscal multiplier in closed economy HANK compared to closed economy RANK models: To the extent that after-tax labor income increases in response to a government spending shock (i.e., that the multiplier channel dominates the tax channel), the closed-economy fiscal multiplier in HANK exceeds the one in RANK—and more so, the more the real interest rate is increased in response to the shock, since this exerts a larger drag on economic activity in the RANK model.

In an open economy, all of these effects are scaled down by a factor  $(1 - \alpha)$ , since a fraction *α* of the additional income is spent on imported goods. All else equal, this therefore tends to reduce the gap between the HANK and RANK multipliers, as compared to a closed economy. In other words, demand leakage abroad reduces the potency of fiscal spending in HANK models.

In addition, the open-economy multiplier is affected by channels 5 and 6, the expenditure switching and real income channels. The former effect—which unambiguously reduces the multiplier relative to the closed-economy case—may be stronger or weaker in the HANK or the RANK model, as its magnitude depends on the size of the domestic boom: A larger boom induces a stronger monetary policy tightening and hence a larger exchange-rate appreciation, which makes households substitute away

<sup>5.</sup> Solving the UIP condition (2) forward yields  $Q_t = \prod_{i=1}^{\infty}$ *k*=0  $\frac{1+r^*}{1+r_{t+k}}$ , with terminal condition  $Q_{\infty}=1$ .



Table 1: Signs of channels in the fiscal multiplier for the RANK and HANK models

Note: The table shows the signs of the contributions of each of the channels from Proposition 1 in the RANK and HANK models. The signs do not indicate whether the channel itself is stronger or weaker, but whether it contributes to a larger or a smaller fiscal multiplier. For example, the interest rate channel is stronger in the RANK model, but since it exerts a negative impact (in both models), it contributes to a larger fiscal multiplier in the HANK model.

from domestic goods on a larger scale. In contrast, the real income channel—which raises the fiscal multiplier—is stronger in the HANK than in the RANK model, as it is scaled by the MPC.

In summary, it is difficult to make general statements about the relative size of the open-economy fiscal multiplier in the HANK and the RANK model. The channels that also exist in a closed economy setting—and there make the fiscal multiplier large in HANK compared to RANK—are weakened in an open economy setting, tending to reduce the gap between fiscal multipliers in HANK compared to RANK. But open economy channels could potentially magnify the gap between HANK and RANK since at least the real income channel is unambiguously larger with heterogeneity than without.

We now proceed by considering some special cases in which the fiscal multipliers in the two models coincide exactly. Using these as starting points, we then consider the relationship between the multipliers in the two models as we depart from these special cases.

# **3.2 Equivalence and the Degree of Openness**

We begin by considering the degree of openness, measured by *α*. We provide an equivalence result, according to which fiscal multipliers coincide in the HANK and RANK models in this case.

**Proposition 2.** *Consider a government spending shock. It then holds that the entire path of*

*output is identical in the RANK and HANK models, i.e.*  $dY_t^{RA} = dY_t^{HA}$  *,*  $\forall t$  *, when* 

 $\alpha \rightarrow 1$ .

*Since the entire path of output is the same, the fiscal multiplier is also the same. In particular,*

$$
d\Upsilon^{RA} = d\Upsilon^{HA} = \begin{cases} 0 & \text{if } \phi_{\Upsilon} > 0 \\ dG & \text{if } \phi_{\Upsilon} = 0 \end{cases}.
$$

*Proof.* See Appendix A.2.

Proposition 2 establishes our first equivalence result regarding the fiscal multiplier in HANK and RANK. It highlights that, as the degree of openness tends to its upper bound of 1 (the opposite of home bias, as the domestic economy consumes only foreign goods), the various forces at play in the two models exactly cancel out. The intuition is that when no domestically produced goods are consumed, the Keynesian multiplier—a defining feature of the HANK model—is shut down completely, since all spending by domestic households goes abroad.

Note that the proposition holds regardless of how fiscal spending is financed, since any change in demand does not affect domestic production at all. The equivalence of fiscal multipliers is also independent of monetary policy: If the central bank responds to the shock by raising the real interest rate ( $\phi$ *Y* > 0), the resulting appreciation of the real exchange rate implies that the expenditure switching channel exactly offsets the increase in government spending, i.e., both models feature a fiscal multiplier of zero. If instead the central bank keeps the real interest rate fixed ( $\phi$ <sup>*y*</sup> = 0), the real exchange rate also remains constant, implying a multiplier of unity in both models (i.e.,  $dY = dG$ ). Monetary policy, therefore, affects the level of the multiplier, but not the relative size across HANK and RANK frameworks.

Finally, since the entire path of output is identical in the two models, an implication is that our equivalence result extends to any measure of the fiscal multiplier, such as the peak multiplier (as studied by Blanchard and Perotti, 2002) or the present-value cumulative multiplier (as proposed by Ramey, 2016).

Figure 1 reports the decomposition of *dY* proposed in Proposition 1 for the case of  $\alpha \rightarrow 1$  studied in Proposition 2. These responses are based on a standard calibration



Figure 1: Decomposition of output (*dY*) when  $\alpha \rightarrow 1$  and  $\phi_Y = 0.25$ 

Note: The figure shows the decomposition of the response of output from Proposition 1 for the HANK and RANK models when  $\alpha \rightarrow 1$  and  $\phi_Y = 0.25$ .

of the remaining model parameters, as discussed in the next section. $6$  The figure confirms that in this case, the increase in government spending is fully crowded out by net exports through the expenditure switching channel, while all other channels are muted, implying a multiplier of zero in both models.<sup>7</sup>

We end this subsection by pointing out that while the limiting case of  $\alpha \rightarrow 1$  may appear less relevant from an empirical viewpoint, as no country purchases zero domestically produced goods, the HANK and RANK multipliers are very similar even for more conventional values of *α*, e.g., around 0.5, as shown in Figure A.2 in Appendix A.2. We return to the quantitative importance of openness when we discuss the fully fledged model.

<sup>6.</sup> The calibration employed in this section differs from the one described in Section 4.2 in a few cases: First, while we target the same MPC throughout the paper, the implied discount factor in our stylized model is  $β = 0.988$ , whereas the model in the next section features discount factor heterogeneity. Second, our assumption of  $r_{ss} \approx 0$  implies  $\mu \approx 1$  in order to ensure a finite price of equity. Finally, we set the monetary policy response to output gap deviations to  $\phi_Y = 0.25$ , and the tax response parameter to  $\phi_G = 0.1$ .

<sup>7.</sup> In the limiting case where the output response approaches zero, the equilibrium responses of the real interest rate and the real exchange rate also approach zero. Thus, in terms of the decomposition in Proposition 1, the real income channel is shut off. However, the expenditure switching channel is scaled by the factor  $\frac{2-\alpha}{1-\alpha}$ , which tends to  $\infty$  as  $\alpha \to 1$ , so that the entire term converges to  $-1$ , as confirmed in Figure 1.

# **3.3 Equivalence and the Trade Elasticity**

We turn now to consider variations in the trade elasticity, *η*, instead of the openness parameter, *α*. While openness measures the magnitude of the reduction in the intertemporal Keynesian multiplier, as discussed above, the trade elasticity determines the strength of the expenditure switching channel. This allows us to establish additional, slightly less general equivalence results.

**Proposition 3.** *Consider a government spending shock, and assume that*  $\phi_Y > 0$ . It *then holds that the entire path of output is identical in the RANK and HANK models, i.e.*  $dY_t^{RA} = dY_t^{HA}$ ,  $\forall t$ , when

 $\eta \rightarrow \infty$ .

*Since the entire path of output is the same, the fiscal multiplier is also the same. In particular,*

$$
d\mathbf{Y}^{RA}=d\mathbf{Y}^{HA}=\mathbf{0}.
$$

*Proof.* See Appendix A.3.

Proposition 3 establishes another case where the fiscal multiplier is identical in the two models, at all horizons. As the trade elasticity approaches infinity, there is full crowding out of the increase in government spending, since the responsiveness of net exports to the real exchange rate tends to infinity. Thus, in equilibrium, the response of the real exchange rate approaches zero as  $\eta \to \infty$ , as does the real interest rate, since output does not move.

Figure 2 summarizes these effects in terms of the decomposition studied above. The figure confirms that output does not respond at any horizon. In the RANK model, the increase in demand from the government is exactly cancelled out by the drop in net exports arising through the expenditure switching channel. In the HANK model, the increase in government spending is counteracted by a small increase in taxes, thus dampening the boom in the domestic economy. The expenditure switching channel is therefore slightly weaker than in the RANK model.

Unlike Proposition 2, the result in Proposition 3 requires an active monetary policy response, i.e.,  $\phi_Y > 0$ . Without such a response, the real interest rate would remain constant, leaving also the real exchange rate unaffected. Thus, the expenditure switching channel would not be active, irrespective of the value of *η*.



Figure 2: Decomposition of output  $(dY)$  when  $\eta \to \infty$ 

Note: The figure shows the decomposition of the response of output from Proposition 1 for the HANK and RANK models when  $\eta \rightarrow \infty$ .

#### **3.3.1 A Special Case: Period-By-Period Financing**

While the previous results hold for any assumption regarding the financing of the increase in government spending, it turns out that another equivalence result between the HANK and RANK multipliers can be obtained in the special case in which the increase in government spending is fully financed on a period-by-period basis, so as to maintain a balanced government budget, i.e., we set  $\phi$ <sup>*G*</sup> = 1 in (9).

**Proposition 4.** *Consider a government spending shock that is financed period-by-period, i.e. dG<sup>t</sup>* = *dT<sup>t</sup>* , ∀*t. In this case, the entire path of output is identical in the RANK and HANK models, i.e.*  $dY_t^{RA} = dY_t^{HA}$ ,  $\forall t$ *, when* 

 $\eta = 1$ .

*Since the entire path of output is the same, the fiscal multiplier is also the same. In particular,*

$$
d\Upsilon^{RA} = d\Upsilon^{HA} = dG - \frac{1}{1-\alpha}Udr, \qquad (13)
$$

*where U is an upper triangular matrix of unit entries.*

*Proof.* See Appendix A.4.

Proposition 4 establishes that, given a balanced government budget, a unitary value of the trade elasticity, *η*, implies that the various forces at play in the two models

exactly cancel out.<sup>8</sup> Why do we obtain equivalence for exactly  $\eta = 1$  and not some other value? Because a unitary trade elasticity is the "Cole-Obstfeld calibration" (since we have log utility, see Cole and Obstfeld, 1991). In this parametrization, the income and substitution effects from changes in the real exchange rate exactly offset each other, so the economy thus behaves almost like a closed economy. In the closed economy, equivalence between HANK and RANK then follows from Werning (2015). We provide more details on this intuition in Appendix A.5.

To shed further light on the mechanics behind this result, Figure 3 shows the decomposition of *dY* proposed in Proposition 1 under the assumptions stated in Proposition 4, i.e.,  $dG_t = dT_t$ ,  $\forall t$ , and  $\eta = 1$ . The figure shows how the different channels exactly cancel out in this case, such that the fiscal multiplier is the same in both models. The additional drag from higher taxes in the HANK model, as compared to the RANK model, is cancelled out by a smaller drag on output due to intertemporal substitution, along with positive contributions from the real income channel and the multiplier channel. Since the magnitude of the domestic boom is the same in the two models, the strength of the expenditure switching channel is equivalent across the two models. As for the magnitude of the multiplier, it is 0.19 in both models, both on impact and when measured by the present-value cumulative multiplier (the two coincide in this case, but not in general). While this number may seem low, it is not inconsistent with empirical estimates for open economies with flexible exchange rates (e.g., Corsetti et al., 2012; Ilzetzki et al., 2013).

#### **3.3.2 The General Case: Partial Financing**

Having considered the limiting case of a balanced budget, we now turn to the more general case where some degree of debt financing is allowed. Tax revenues are assumed to follow equation (9)—which in linear form reads  $dT_t = \phi_G dG_t$ —with  $\phi_G \in [0,1]$ . We now explore the potential existence of values of *η* that establish equivalence between multipliers across HANK and RANK models for arbitrary values of  $\phi_G$ . To this end, we resort to a numerical analysis, in which we focus on the

<sup>8.</sup> A unitary trade elasticity is consistent with the existing empirical literature. For example, recent estimates by Boehm et al. (2023) suggest a short-run trade elasticity of 0.76, increasing to 1 after three-four years, and around 2 after a decade.



Figure 3: Decomposition of output (*dY*) when *η* = 1

Note: The figure shows the decomposition of the response of output from Proposition 1 for the HANK and RANK models when  $\eta = 1$  and the government maintains a balanced budget.

present-value cumulative fiscal multiplier up to some horizon *T*, defined as:

$$
\mathcal{M}^{j} \equiv \frac{\sum_{t=0}^{T} \frac{dY_{t}^{j}}{(1+r)^{t}}}{\sum_{t=0}^{T} \frac{dG_{t}}{(1+r)^{t}}}.
$$
\n(14)

In practice, we compute the multiplier over 5 years (i.e.  $T = 20$ ) for a range of values of  $\phi$ <sup>*G*</sup> and *η* for each of the two models. The results are reported in Figure 4, which shows the difference between the multipliers in the two models, i.e.,  $\mathcal{M}^{\text{HA}} - \mathcal{M}^{\text{RA}}$ .<sup>9</sup> The green area indicates tuples  $(\phi_G, \eta)$  for which the HANK fiscal multiplier is larger than the RANK fiscal multiplier, i.e.  $\mathcal{M}^{HA} > \mathcal{M}^{RA}$ . The red area, instead, indicates tuples ( $\phi_G$ , $\eta$ ) where the RANK fiscal multiplier is larger, i.e.  $\mathcal{M}^{RA} > \mathcal{M}^{HA}$ . The black line indicates the border between these to areas, i.e. where  $\mathcal{M}^{RA} = \mathcal{M}^{HA}$ . Note that the black line crosses through the limiting case studied in Proposition 4, i.e.,  $(\phi_G, \eta) = (1, 1)$ , whereas it converges to the case from Proposition 3, i.e.,  $\eta \to \infty$ . By "connecting the dots", the black line shows that equivalence between the two multipliers can be established numerically for intermediate values of *ϕ<sup>G</sup>* and *η*.

<sup>9.</sup> We report the multiplier for each model separately in Figure A.5. While Propositions 2, 3, and 4 provided equivalence results for the response of output at all points in time, i.e.  $dY_t^{HA} = dY_t^{RA}$ ,  $\forall t$ , Figure 4 only establishes equivalence for the present-value cumulative multiplier. This implies that the paths of output might differ across models, even if the multiplier is the same. We have verified that the figure looks very similar if we focus on the impact or the peak multiplier instead of the present-value cumulative multiplier.

To understand the results in Figure 4, consider first variations in the degree of financing,  $\phi_G$ . A reduction in the degree of financing, i.e., a drop in  $\phi_G$ , implies a smaller increase in taxes. This entails that the negative impact of the tax channel on consumption in the HANK model is weakened, so the HANK multiplier is more likely to exceed the RANK multiplier, all else equal, as indicated by moving left towards the green area (or further away from the red area), for a given value of *η*.

Next, consider variations in the trade elasticity, *η*, holding *ϕ<sup>G</sup>* fixed. As the trade elasticity increases, expenditure switching becomes more important in both models, which reduces the fiscal multiplier in both cases. Furthermore, the smaller increase in output weakens the intertemporal Keynesian multiplier present in the HANK model.<sup>10</sup> As a result, an increase in  $\eta$  exerts a stronger negative effect on the fiscal multiplier in the HANK model than in the RANK model, consistent with moving towards the red area (or further away from the green area).

What can we say about the magnitude of the gap in fiscal multipliers? Anticipating the results from the quantitative models, we note that the difference between the fiscal multipliers in the HANK and RANK models in Figure 4 is small for any calibration. In particular, the largest difference is around 0.1 for pure debt-financing, with values even closer to 0 for any other calibration.

### **3.4 Summary**

To sum up this section, we have documented that the same six channels are at play in response to fiscal policy shocks in open-economy HANK and RANK models. However, their magnitude—and potentially their sign—has been shown to vary across models. This paves the way for equivalence results, where the channels cancel each other out, leading to equivalence of output and fiscal multipliers in the two models. We have provided a set of such results, where the entire paths of output, and hence the fiscal multipliers, are the same in the HANK and RANK models.

<sup>10.</sup> Analytically, this can be seen by collecting the  $dY$ <sup>*j*</sup>-terms in the expression in Proposition 1 and then solving for  $dY^j$ , which entails that the expenditure switching term gets premultiplied by  $[I - (1 - \alpha)M^j]^{-1}$ , where *I* is the identity matrix. Thus, the effect on output of a change in *η* is seen to scale with the MPCs, as reflected by the matrix *M<sup>j</sup>* .



Figure 4: Difference between fiscal multipliers in HANK and RANK

Note: The figure shows the difference in cumulative fiscal multipliers between the HANK and RANK models in the stylized setting, i.e.  $\tilde{M}^{HA} - M^{RA}$ , for a range of values of the trade elasticity (*η*) and the degree of financing ( $\phi_G$ ). The cumulative fiscal multiplier is computed over 5 years, i.e.  $T = 20$  in (14).

# **4 Numerical Results**

Motivated by the equivalence results established in the previous section, we now turn to a quantitative assessment of the fiscal multiplier in the HANK and RANK models, with the aim of exploring whether these remain relatively similar for realistic calibrations.

# **4.1 Quantitative Model Elements**

We extend the stylized model described in Section 2 with a number of elements to make it more realistic from a quantitative viewpoint. In particular, we consider four new model elements: Permanent discount factor heterogeneity, time-varying trade elasticities, a more elaborate government sector, and a fixed cost in production.

#### **4.1.1 Permanent Discount Factor Heterogeneity**

We introduce permanent heterogeneity in household discount factors: Half of the households are impatient with discount factor, *β* low, while the remaining households are patient with discount factor, β<sup>high</sup>. This allows us to simultaneously match the

MPC (as in the stylized model) along with a realistic level of government debt (in contrast to the stylized model). Households of both types solve the same problem as in the stylized model, but with (permanently) different discount factors.  $<sup>11</sup>$ </sup>

#### **4.1.2 Time-Varying Trade Elasticities**

Following recent advances in the trade literature (see Drozd et al., 2021 and Boehm et al., 2023), we allow for a dynamic trade elasticity, which is low in the short run but high in the long run. Specifically, we assume that the domestic CES demand for imports and the Armington demand for exports are given by:

$$
C_{F,t} = \alpha (\hat{p}_t)^{-\eta} C_t, \quad \hat{p}_t = (\hat{p}_{t-1})^{\rho_{\eta}} \left(\frac{P_{F,t}}{P_t}\right)^{1-\rho_{\eta}}, \tag{15}
$$

$$
C_{H,t}^* = \alpha^* \left(\hat{p}_t^*\right)^{-\eta} C_t^*, \quad \hat{p}_t^* = \left(\hat{p}_{t-1}^*\right)^{\rho_\eta} \left(\frac{P_{H,t}^*}{P_t^*}\right)^{1-\rho_\eta},\tag{16}
$$

where  $\rho_{\eta} \in [0,1)$  captures the smoothness embedded in the process. We retrieve a constant trade elasticity when  $\rho_{\eta} = 0$ .

#### **4.1.3 Government**

We expand on the reaction of the monetary policy authority. In particular, we now consider a Taylor rule featuring an inflation response and interest rate smoothing:

$$
i_t = \rho_i i_{t-1} + (1 - \rho_i) \left( i_{ss} + \phi_\pi \pi_t + \phi_Y \left[ \frac{Y_t}{Y_{ss}} - 1 \right] \right). \tag{17}
$$

Furthermore, we consider a tax rule reacting to the lagged level of debt:

$$
T_t = T_{ss} + \phi_B (B_{t-1} - B_{ss}), \qquad (18)
$$

reminiscent of Galí (2020). Unlike the rule employed in Subsection 3.3.2, this rule ensures that government debt returns to its original steady state.

<sup>11.</sup> In the NKWPC (7), we use the average discount factor:  $(\beta^{\text{low}} + \beta^{\text{high}})/2$ .

#### **4.1.4 Fixed Cost**

Finally, we introduce a fixed cost in production in order to be able to simultaneously obtain a realistic markup and a level of aggregate wealth to GDP consistent with the data. In particular, firm profits are now:

$$
D_t = (1 - \tau_t) \frac{P_{H,t} Y_t - W_t N_t}{P_t} - F,
$$
\n(19)

where *F* is the fixed cost. Goods market clearing then becomes

$$
Y_t = C_{H,t} + C_{H,t}^* + G_t + \frac{P_t}{P_{H,t}} F.
$$
\n(20)

With no fixed cost, a realistic markup would imply an implausibly high wealth level.

# **4.2 Calibration**

Our calibration follows the one of Druedahl et al. (2022) on most dimensions, but adapted for a one-sector model. Thus, the calibration targets the average small open economy in a sample of OECD countries. The baseline calibration of the model is summarized in Table 2.

Regarding household preferences, we set the inverse of the Frisch elasticity to  $\varphi = 2$ . We set the discount factor of patient households to match an annual real interest rate of 2%, as discussed in Druedahl et al. (2022). The discount factor of impatient households is set to match an annual MPC of 0.51, following Fagereng et al. (2021). We take the parameters governing the idiosyncratic component of income from Druedahl et al. (2022), who use standard values from Floden and Lindé (2001). The calibration of the representative agent model differs regarding the discount factor, which is given by  $1/(1 + r)$ .

On the firm side, we opt for a markup of 20%. We then set the fixed cost to ensure that the total supply of assets yields an aggregate ratio of assets to output (*A*/*Y*) of 10 (2.5 annually) as in Druedahl et al. (2022). The slope of the wage Philips curve is set to 0.05, as in Druedahl et al. (2022).



#### Table 2: Calibration

Note: The table summarizes the baseline parameter values. B23 is Boehm et al. (2023). C11 is Chetty et al. (2011). D22 is Druedahl et al. (2022). F21 is Fagereng et al. (2021). FL01 is Floden and Lindé (2001). G20 is Galí (2020). HMM19 is Hagedorn et al. (2019). OECD refers to data from the OECD for the sample in Druedahl et al. (2022).

For the government, we set the steady state values of government consumption and debt to match the OECD data, giving us  $G_{ss} = 0.2$  and  $B_{ss} = 2.32$  (implying a debt-to-GDP ratio of 58% annually), as steady-state output is normalized to 1. The steady-state level of tax revenues then follows residually. Regarding the financing of spending shocks, we set  $\phi_B = 0.02$  following Galí (2020), implying that increases in government spending are financed mostly by higher public debt in the short run, with taxes responding very slowly. We assume that the government spending shock follows an AR(1) process with persistence  $\rho_G = 0.9$ , following Hagedorn et al. (2019). Monetary policy is assumed to respond to consumer price inflation with a coefficient of  $\phi_{\pi} = 1.5$ , whereas we set the output-gap response to zero,  $\phi_{\Upsilon} = 0$ , as a baseline. The interest-rate smoothing parameter is set to 0.9.

Finally, regarding the foreign economy, we assume a net foreign asset position of zero in the steady state, such that trade is initially balanced. We calibrate the foreign share of consumption (*α*) to match an import-to-GDP ratio of 42%, corresponding to the average across OECD countries. As in Druedahl et al. (2022), we calibrate the (long-run) trade elasticity, *η*, and the rigidity in substitution, *ρη*, to match the evidence from Boehm et al. (2023). This yields  $\eta = 2$  and  $\rho_{\eta} = 0.9$ .

#### **4.3 Baseline Results**

The impulse-response functions (IRFs) to a government spending shock in both the HANK and the RANK model are shown in Figure 5. As the figure shows, the response of GDP is very similar in the two models, though slightly larger—and more shortlived—in the HANK model. The impact multiplier is 1.11 in the HANK model and 0.93 in the RANK model, whereas the present-value cumulative multiplier is 0.39 and 0.45, respectively, when considering the first 20 quarters after the shock (see Table 3). Overall, the main insight from the previous section is therefore confirmed: the open-economy fiscal multiplier is relatively similar across HANK and RANK models. The underlying dynamics, however, is quite different. The HANK model displays a large increase in domestic consumption, reflecting the high MPC displayed by households in this economy. As anticipated in the analytical results, part of the increase in consumption is directed towards foreign goods, leading to a notable increase in imports and, in turn, a decline in net exports. In the RANK model, in contrast, domestic consumption declines, since the MPC in this economy is low, and households instead postpone consumption in response to the increase in the real interest rate (except for the first few quarters). This spills over into a drop in imports, and therefore an increase in net exports in the RANK economy. In the aggregate, the different responses of consumption and net exports in the two models roughly cancel out, explaining the relatively similar dynamics of output. The real interest rate and the real exchange rate display relatively similar patterns in the two models: the real interest rises, except for an initial decline due to nominal interest-rate smoothing, while the real exchange rate appreciates. Finally, the pattern of government debt is



Figure 5: IRFs to a government consumption shock

Note: The figure shows impulse response functions to a government consumption shock in the baseline model.

almost identical in the two models.

# **4.4 Alternative Model Specifications**

We now consider several extensions of the baseline framework and their implications for fiscal multipliers, both to investigate the sensitivity of the baseline results and to provide more intuition. The fiscal multipliers associated with each of the experiments are collected in Table 3.

**Monetary policy** In order to check the sensitivity of our main insights, we first explore alternative assumptions regarding monetary policy. We begin by treating the case of a fixed exchange rate, i.e., where the Taylor rule (17) is replaced by a rule that keeps the *nominal* exchange rate fixed at all time, i.e.  $E_t = E_{ss}$ . The IRFs of the most important variables are reported in Figure 6 (top row). The responses are very similar to those observed under a floating exchange rate, implying that the fiscal multipliers



Figure 6: IRFs to a government consumption shock: Sensitivity checks

Note: The figure shows impulse response functions to a government consumption shock under various model assumptions regarding monetary policy (rows 1-3) and the trade elasticity (rows 4-5).

are also barely affected, as seen from Table 3.<sup>12</sup>

<sup>12.</sup> The response of the real interest rate is quite similar across exchange-rate regimes. Under a peg, the central bank keeps the nominal interest rate fixed. The path of the real interest rate is then determined by the dynamics of consumer price inflation, which first increases in response to higher domestic prices, but then declines due to expenditure switching towards cheaper foreign goods.

We then consider the case of a more aggressive response of monetary policy, implemented by setting  $\phi_{\pi} = 2$  and  $\phi_{\gamma} = 1$ . A stronger increase in the real interest rate implies a larger appreciation of the real exchange rate. In the HANK model, this strengthens both the real income channel (leading to a stronger increase in domestic consumption) and the expenditure switching channel (leading to larger drop in net exports). But again, the negative comovement between these two variables leads to a muted effect on output, which therefore remains fairly similar in the two models, as seen from Figure 6 (row two). Another alternative is a "passive" monetary policy rule, according to which the central bank keeps the real interest rate fixed at all times, i.e.  $r_t = r_{ss}$ . Such a rule implies a slightly higher impact multiplier than our baseline model (see Figure 6, row three).  $^{13}$ 

All in all, we see that the relative size of the fiscal multiplier is not substantially affected by monetary policy. The reason is that demand for both domestic and foreign goods is affected symmetrically, and so their high correlation in the models is largely preserved. In the HANK model, a positive domestic consumption response continues to be offset by a matching increase in imports, thus muting any overall change in the fiscal multiplier.

**The trade elasticity** Given the considerable uncertainty surrounding estimates of the trade elasticity in the existing literature, and the central role of this parameter for the transmission of shocks to consumption in HANK and RANK models established by Auclert et al. (2021b), we also consider variations of *η*. In particular, we first consider a higher value of the long-run elasticity, with  $\eta = 4$ , and then a trade elasticity that is not dynamic, i.e. we set  $\rho_{\eta} = 0$  (so that the value of  $\eta$  is constant at 2). The resulting IRFs are shown in Figure 6 (rows four and five).

A higher trade elasticity has a very modest impact on our results, reducing the fiscal multiplier slightly in both models due to a stronger expenditure switching effect. The relative fiscal multiplier is largely unchanged. A static trade elasticity works in the same direction, but exerts a more powerful effect, reflecting that changes in the short-run trade elasticity are stronger than long-run changes. However, since the HANK and RANK multipliers are reduced in parallel, they remain quite similar. Changes in the trade elasticity do not affect the leakage of demand abroad more in HANK than in RANK.

<sup>13.</sup> In fact, the cumulative multipliers in the HANK and RANK models are identical and equal to 1 over the entire horizon, i.e., as  $T \to \infty$  in (14), as established analytically in Sundram (2024).

**Openness** While monetary policy and the trade elasticity do not substantially affect the relative size of the fiscal multiplier in our models, openness matters somewhat more. This can be observed from Figure 7 (rows one and two), where we consider variations in the openness parameter, *α*. <sup>14</sup> In the HANK model, the fiscal multiplier is lower when the economy is more open, and vice versa. Building on the intuition from the stylized model, this reflects that the leakage of domestic demand abroad is more important when the degree of openness is higher. Since the RANK multiplier is less sensitive to variations in *α*, we therefore observe a larger difference between the two multipliers when the economy is less open.

**Sticky prices** The nature of nominal rigidities matters for the relative fiscal multiplier across HANK and RANK. While our assumption of sticky wages is consistent with most of the existing HANK literature (e.g., Hagedorn et al., 2019 and Auclert et al., 2023), models in the RANK tradition have typically focused on sticky prices (e.g., Galí and Monacelli, 2005), and Broer et al. (2023) show that this choice is not innocuous for fiscal multipliers.

We add sticky prices by replacing the pricing equation,  $P_{H,t} = \mu W_t$ , with the following New-Keynesian Phillips Curve (NKPC):

$$
\pi_{H,t} = \kappa_H \left( \frac{W_t}{P_{H,t}} - \frac{1}{\mu} \right) + \beta \pi_{H,t+1}.
$$

We set  $\kappa_H = 0.15$  following Druedahl et al. (2022). We first consider the case with sticky prices and flexible wages, i.e.  $\kappa \to \infty$ .

As seen from Figure 7 (row three), this widens the gap between HANK and RANK multipliers more than in the other sensitivity checks we have conducted, at least on impact. Under this specification, firm profits become countercyclical, and real wages display a stronger increase, boosting the consumption response in HANK. At the same time, however, since prices are rigid, the real exchange rate is less responsive. Thus, in this case unlike all the others we have considered so far, the correlation between consumption and imports becomes weaker, with the rise in consumption substantially stronger than the drop in net exports, implying a larger output response in HANK. In the RANK model, instead, the increase in real wages cancels out with the drop in profits, from the viewpoint of the representative household, so the RANK

<sup>14.</sup> The values of *α* considered here are calibrated to obtain import-to-GDP ratios of 26% and 52%, respectively, corresponding to the first and third quartile across our sample of OECD countries.



Figure 7: IRFs to a government consumption shock: Sensitivity checks (continued) Note: The figure shows impulse response functions to a government consumption shock under various model assumptions regarding openness (rows 1-2) and nominal rigidities (rows 3-4).

response is very similar to the baseline. In the empirically plausible case where wages are more sticky than prices—and profits are procyclical—fiscal multipliers are instead very close to the baseline (see the bottom row of Figure 7).

### **4.4.1 The Role of Financing**

Our analytical results hinted at the importance of the role of financing—together with the trade elasticity—in driving the size of the fiscal multiplier in HANK. The previous literature has established that, in the context of HANK models, the timing of the increase in taxes required to finance the additional government spending plays a crucial role for the size of fiscal multipliers (see, e.g., Hagedorn et al., 2019 and Auclert et al., 2023). This is in contrast to the literature based on representativeagent models, where some form of Ricardian equivalence typically applies. Thus, one may suspect that alternative financing assumptions could break the similarity between HANK and RANK multipliers established above. To explore this aspect in the quantitative framework, we now consider a variety of financing rules proposed in the existing literature, and their implications for fiscal multipliers. Specifically, we employ the following rules: i) Following Galí et al. (2007), we assume that taxes adjust to contemporaneous debt and public spending according to

$$
dT_t = \phi_B dB_t + \phi_G dG_t,
$$

with  $\phi_B = 0.33$  and  $\phi_G = 0.1$ . ii) Following Auclert et al. (2023), we assume that taxes adjust such that public debt satisfies

$$
dB_t = \phi_B(dB_{t-1} + dG_t),
$$

with  $\phi_B = 0.93$ . iii) Following Hagedorn et al. (2019), we assume that taxes are fixed initially, and then phased in after a while in order to stabilize the debt level:

$$
T_t = \begin{cases} T_{ss} & \text{if } t < t_B, \\ (1 - \omega) T_{ss} + \omega \tilde{T}_t & \text{if } t \in [t_B, t_B + \Delta_B], \\ \tilde{T}_t & \text{if } t > t_B + \Delta_B, \end{cases}
$$

where  $\tilde{T}_t=T_{ss}\left(\frac{B_{t-1}}{B_{ss}}\right)$ , and where  $t_B=50$  and  $\Delta_B=20.^{15}$  iv) Finally, we consider a balanced budget rule, such that  $B_t = B_{ss}$  for all *t*.

The IRFs to a government spending shock under these financing schemes are reported in Figure 8, where the different cases have been ordered according to the magnitude of the implied increase in government debt, as seen from the right column. The various fiscal rules have notably different implications for the path of government debt: In the first three rows, the increase in government debt is smaller than in our baseline model, implying a larger increase in taxes, which dampens the increase in consumption in the HANK model. An extreme case of this is seen under a balanced budget, where a drop in consumption can be observed (top row). In contrast, the

<sup>15.</sup> In the practical implementation,  $\omega$  is a function of  $x = \left(\frac{t-t_B}{\Delta_B}\right)$ ), with  $\omega(x) = 3x^2 - 2x^3$ .



Figure 8: IRFs to a government consumption shock with different financing schemes

Note: The figure shows impulse response functions to a government consumption shock under a range of different assumptions regarding the financing of the increase in spending. GLV07 is Galí et al. (2007), ARS23 is Auclert et al. (2023), and HMM19 is Hagedorn et al. (2019).

bottom row shows a rule where government debt displays a larger increase, boosting the response of consumption.

The key insight from this exercise, however, is that the response of output displays only very small changes as we vary the financing rule. As seen from Table 3, the impact multipliers are barely affected by this choice, and remain very similar in the HANK and RANK models, whereas the cumulative multipliers are somewhat more responsive, though without altering the main picture. The explanation is that the response of net exports tends to mirror that of private consumption; declining by more when consumption increases by more, and vice versa, partly because a fraction of the increase in consumption is directed towards foreign goods, and partly due

to expenditure switching resulting from the appreciation of the real exchange rate. In terms of our results from the stylized model, in an open economy the financing channel is not as important in driving the relative size of the fiscal multiplier since that channel is scaled down by openness; what is important instead is the degree to which demand leaks abroad, that is, increased consumption demand is spent on imports, which is unaffected by the choice of financing.

#### **4.4.2 The Response of the Real Exchange Rate**

In our model, the real exchange rate is determined through the UIP condition, given a path for monetary policy. As seen above, our baseline model features an appreciation of the real exchange in response to a government spending shock, consistent with the idea that a fiscal expansion drives up the relative price of domestic goods. In the existing empirical literature, however, this response is at the centre of a long-standing debate, with several authors reporting evidence of a—counterintuitive—depreciation of the real exchange rate (see, e.g., Kim and Roubini, 2008, Monacelli and Perotti, 2010, and Ravn et al., 2012). More recent contributions have challenged or modified this result somewhat (see, e.g., Ferrara et al., 2021 or Born et al., 2024, who also provide surveys of this literature). While we do not wish to take a stand on this question, we find it important to document that our theoretical insight is not sensitive to the conditional response of the real exchange rate. To this end, we allow for UIP deviations in the form of a UIP shock,  $\varepsilon_t^{\text{UIP}}$ *t* . This implies that the real UIP condition (2) is modified to:  $16$ 

$$
1 + r_t = (1 + r^*) \frac{Q_{t+1}}{Q_t} + \varepsilon_t^{\text{UIP}}.
$$

We can then back out the path for  $\varepsilon_t^{\text{UIP}}$  $t_t^{\text{UP}}$  required to obtain any desired response of the real exchange rate.<sup>17</sup> We consider two cases: One where the UIP shock ensures that the real exchange rate remains constant,  $dQ_t = 0$  for all *t*, and another where the UIP deviation is such that the real exchange rate moves exactly opposite the baseline case, i.e., it depreciates by the same amount that it appreciates in the baseline.

<sup>16.</sup> We also adjust the asset returns,  $r_t^a$ , to reflect that returns are not equalized even after period 0 due to the UIP deviation.

<sup>17.</sup> We have opted for this reduced-form approach to obtain a depreciation of the real exchange rate. Structural mechanisms proposed in the literature to obtain such a response include spending reversals (Corsetti et al., 2010) and deep habits (Ravn et al., 2012).

The implied IRFs are reported in Figure 9. As compared to the baseline case of an appreciation from Figure 5, a constant real exchange rate implies a boost to net exports through expenditure switching, so that net exports display a clear increase in both models (row one). This effect is even stronger in the case of a depreciation (row two). However, in both cases, the increase in net exports is counteracted by a decline in domestic consumption. In the HANK model, this reflects a reversal of the powerful real income channel, as domestic households are poorer in real terms. In the RANK model, the drop in consumption is due to the increase in the domestic real interest rate resulting from the UIP shock. In other words, both models display a negative comovement between domestic consumption and net exports. As seen from the figure, the response of output is very similar in the HANK and RANK models, irrespective of the response of the real exchange rate.<sup>18</sup>

#### **4.4.3 Model with Capital**

Finally, we can show that introducing capital into the model does not affect our main message. Assume that the production function of domestic firms is given by  $Y_t =$  $N_t^{1-\alpha_K} K_{t-}^{\alpha_K}$ *t*−1 . The capital stock is owned by capital firms, and evolves according to a standard law of motion. Capital firms are subject to quadratic investment adjustment costs. The details are presented in Appendix B. We set the capital share  $(\alpha_K)$  to a standard value of 0.33, while the depreciation rate of capital is 1.25% per quarter. The IRFs to a government spending shock in the models with capital are shown in Figure 9 (bottom row). The introduction of capital reduces the fiscal multiplier, as investment displays a clear decline in both models (while leaving the dynamics of consumption and net exports largely unaffected, relative to the baseline case). However, the dynamics of output remains very similar across the HANK and RANK economies, with present-value cumulative multiplier of 0.22 and 0.26, respectively. In other words, the introduction of capital does not materially affect our main message.

<sup>18.</sup> While the impact multipliers from each model display a modest sensitivity with respect to movements in the real exchange rate, as seen from Table 3, the cumulative multipliers are significantly larger when the UIP shock is active, as compared to the baseline model, since the increase in output becomes more persistent in these cases.



Figure 9: IRFs to a government consumption shock: Sensitivity checks (continued) Note: The figure shows impulse response functions to a government consumption shock under various model assumptions regarding deviations from the UIP (rows 1-2) and with capital formation (row 3).

# **5 Conclusion**

We have studied fiscal multipliers in a small open economy Heterogeneous Agent New-Keynesian model, and compared the fiscal multipliers in this model to those from a representative-agent model. Our general takeaway is that fiscal multipliers are similar in both types of models. This result is based on two types of arguments. First, we have established analytical equivalence results in a stylized setting, and second, we have shown that fiscal multipliers are generally quite similar in a quantitative model. These results are in contrast with those for a closed economy, where the introduction of households with sizeable marginal propensities to spend have been shown to boost fiscal multipliers. The difference arises primarily from demand leakage abroad: Even though in the HANK framework consumption demand is boosted more than in the RANK setting, this increased demand is spent partly on imports, thus weakening the impact of the fiscal stimulus on domestic output. Factors like monetary policy and financing play a limited quantitative role in determining the relative size of the fiscal

multiplier in open economy HANK compared to RANK.

In the quantitative setting, we have shown that fiscal multipliers are generally at most 20 percent larger in HANK than in RANK, and that the absolute size of fiscal multipliers displays limited sensitivity to the various model perturbations we considered. The fiscal multiplier is close to 1 on impact in the models we have considered, while the cumulative multiplier is between zero and 0.5, with few exceptions. This is consistent with a boom-bust type of pattern in consumption and output: Output initially rises following higher government spending, but after a while consumption drops to pay back debt to foreigners.

The focus of our analysis has been on the *relative* magnitude of multipliers in HANK and RANK models, and less on the absolute size of these. Likewise, the fact that impact multipliers are generally higher than cumulative multipliers in the models we have considered reflects—at least partly—the absence of model ingredients aimed at obtaining the hump-shaped impulse responses often observed in applied work. Thus, we leave for future research a more detailed assessment of the ability of the models considered above to provide a quantitative account of the empirical effects of fiscal policy in small open economies.



# Table 3: Fiscal multipliers in different models

Note: The table reports impact and cumulative fiscal multipliers from the HANK and RANK models (and the difference between these) for a range of different modeling assumptions. The cumulative fiscal multiplier is computed over 5 years, i.e.  $T = 20$  in (14).

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# **Appendix**

# **A Stylized Model Appendix**

In the following, we present the proofs of each of the propositions in Section 3 in the main text.

### **A.1 Proof of Proposition 1**

We begin by linearizing some key equations that we use to prove the proposition.

#### **A.1.1 Domestic Consumption of Home Goods**

Linearizing the CPI in (4) yields

$$
dP_t = \alpha dP_{F,t} + (1 - \alpha)dP_{H,t}.
$$
\n(21)

Next, linearizing the nominal exchange rate yields

$$
dE_t = dP_{F,t}.\tag{22}
$$

Similarly, linearizing the definition of the real exchange rate implies that

$$
dQ_t = dE_t + dP_t^* - dP_t. \tag{23}
$$

Inserting (22) into (23) yields

$$
dQ_t = dP_{F,t} - dP_t^* + dP_t^* - dP_t = dP_{F,t} - dP_t.
$$

Solving for *dPF*,*<sup>t</sup>* , we find that

$$
dP_{F,t} = dQ_t + dP_t. \tag{24}
$$

Inserting this into the linearized CPI (21) and solving for  $dP_{H,t} - dP_t$ , we obtain

$$
dP_{H,t} - dP_t = -\frac{\alpha}{1-\alpha} dQ_t.
$$
\n(25)

Linearizing domestic consumption of home goods (3) gives

$$
dC_{H,t} = (1 - \alpha) [dC_t - \eta (dP_{H,t} - dP_t)].
$$

Inserting (25) yields

$$
dC_{H,t} = (1 - \alpha)dC_t + \eta \alpha dQ_t.
$$
 (26)

### **A.1.2 Foreign Consumption of Home Goods**

Linearizing *P* ∗ *H*,*t* in (5) gives

$$
dP_{H,t}^* = dP_{H,t} - dE_t.
$$

Insert now (22) to get that

$$
dP_{H,t}^* = dP_{H,t} - dP_{F,t}.
$$

Inserting (24) yields

$$
dP_{H,t}^* = dP_{H,t} - dP_t - dQ_t.
$$

Insert finally (25) to obtain

$$
dP_{H,t}^* = -\frac{1}{1-\alpha} dQ_t.
$$
\n<sup>(27)</sup>

Linearizing foreign consumption of home goods in (11) gives

$$
dC_{H,t}^* = -\eta \alpha dP_{H,t}^*.
$$

Insert (27) to get that

$$
dC_{H,t}^* = \frac{\eta \alpha}{1 - \alpha} dQ_t.
$$
 (28)

#### **A.1.3 The Linearized Consumption Function**

The linearized consumption function is

$$
dC = C^Z dZ + C^r dr + C^{r^a} dr_0^a,
$$
\n(29)

with Jacobians

$$
C^Z \equiv \frac{\partial C}{\partial Z}, \quad C^r \equiv \frac{\partial C}{\partial r}, \quad C^{r^a} \equiv \frac{\partial C}{\partial r^a_0}.
$$

Insert now  $W_t = P_{H,t}/\mu$  into the definition of labor income to get that

$$
Z_t = (1 - \tau_t) \frac{1}{\mu} \frac{P_{H,t}}{P_t} Y_t.
$$

Taking a first-order approximation of this yields

$$
dZ_t = (1 - \tau) \frac{1}{\mu} (dY_t + dP_{H,t} - dP_t) - \frac{1}{\mu} d\tau_t
$$
  
= 
$$
(1 - \tau) \frac{1}{\mu} \left( dY_t - \frac{\alpha}{1 - \alpha} dQ_t \right) - \frac{1}{\mu} d\tau_t,
$$

where we have used (25) in the second line. Inserting this into the linearized consumption function in (29), it follows that

$$
d\mathbf{C} = (1-\tau)\frac{1}{\mu}\mathbf{C}^Z \left(d\mathbf{Y} - \frac{\alpha}{1-\alpha}d\mathbf{Q}\right) - \frac{1}{\mu}\mathbf{C}^Z d\tau + \mathbf{C}^r dr + \mathbf{C}^{r^a} dr_0^a.
$$
 (30)

To proceed we use that the valuation effect at time 0 is given by  $r_0^a = \frac{p_0^D + D_0}{p_{\rm sc}^D}$  $\frac{P_{\textit{DS}}}{p_{\textit{ss}}^D} - 1$ . If we iterate forward on the equity pricing condition, we have:

$$
p_t^D = \frac{D_{t+1}}{1+r_t} + \frac{D_{t+2}}{(1+r_t)(1+r_{t+1})} + \frac{D_{t+3}}{(1+r_t)(1+r_{t+1})(1+r_{t+2})} \cdots
$$

implying that that the equity price is a function of the sequences of dividends and real interest rates;  $p_t^D = p_t^D \left( \{D_s, r_s\}_{s=1}^{\infty} \right)$  $\int_{s=0}^{\infty}$ ). Since  $r_0^a$  is a function of dividends and the equity price, we also have  $r_0^a = r_0^a \left( \{D_s, r_s\}_{s=0}^{\infty} \right)$  $\int_{s=0}^{\infty}$ ). Linearizing  $r_0^a$  w.r.t. inputs*,* we then obtain:

$$
dr_0^a = \frac{r_{ss}}{D_{ss}} \left( dD_0 + \frac{dD_1}{1+r} + \frac{dD_2}{(1+r)^2} + \frac{dD_3}{(1+r)^3} \cdots \right) - \frac{D_{ss}}{p_{ss}^D} \left( dr_0 \frac{1}{(1+r)} \sum_{s=0}^{\infty} \frac{1}{(1+r)^{1+s}} + dr_1 \frac{1}{(1+r)^2} \sum_{s=0}^{\infty} \frac{1}{(1+r)^{1+s}} + \cdots \right).
$$

We can then use  $p_{ss}^D = \frac{D_{ss}}{r_{ss}}$  $\frac{D_{ss}}{r_{ss}}$  and  $\frac{1}{1+r}\sum_{s=0}^{\infty}\left(\frac{1}{1+r}\right)$ 1+*r*  $\int^{s} = \frac{1}{1+r}$ 1  $\frac{1}{1-\frac{1}{1+r}} = \frac{1}{1+r}$  $\frac{1+r}{r} = \frac{1}{r}$  to obtain

$$
dr_0^a = \frac{r_{ss}}{D_{ss}} \left( dD_0 + \frac{dD_1}{1+r} + \frac{dD_2}{(1+r)^2} + \frac{dD_3}{(1+r)^3} \cdots \right) - \left( dr_0 \frac{1}{(1+r)} + dr_1 \frac{1}{(1+r)^2} - \cdots \right).
$$

We can define the following vectors:

$$
J'_{D} = \frac{r_{ss}}{D_{ss}} \left( 1, \frac{1}{1+r}, \frac{1}{(1+r)^2}, \dots \right)
$$
  

$$
J'_{r} = -\left( \frac{1}{(1+r)}, \frac{1}{(1+r)^2}, \frac{1}{(1+r)^3}, \dots \right),
$$

to get

$$
dr^a = J'_r dr + J'_D dD.
$$

Using  $P_{H,t} = \mu W_t$  and  $Y_t = N_t$ , we can write dividends as:

$$
D_t = (1 - \tau_t) \frac{P_{H,t} Y_t - \frac{1}{\mu} P_{H,t} Y_t}{P_t} = (1 - \tau_t) \left( 1 - \frac{1}{\mu} \right) \frac{P_{H,t}}{P_t} Y_t,
$$

or in sequence space:

$$
d\mathbf{D} = (1 - \tau_{ss}) \left( 1 - \frac{1}{\mu} \right) (d\mathbf{P}_{\mathbf{H}} - d\mathbf{P} + d\mathbf{Y}) - \left( 1 - \frac{1}{\mu} \right) d\tau
$$
  
=  $(1 - \tau_{ss}) \left( 1 - \frac{1}{\mu} \right) \left( d\mathbf{Y} - \frac{\alpha}{1 - \alpha} d\mathbf{Q} \right) - \left( 1 - \frac{1}{\mu} \right) d\tau.$ 

where the last line uses (25). Returning to the consumption function, (30), we then get:

$$
dC = (1 - \tau_{ss}) \frac{1}{\mu} C^Z \left( d\Upsilon - \frac{\alpha}{1 - \alpha} dQ \right) - \frac{1}{\mu} C^Z d\tau + C^r dr + C^r dr_0^a
$$
  
=  $(1 - \tau_{ss}) \frac{1}{\mu} C^Z \left( d\Upsilon - \frac{\alpha}{1 - \alpha} dQ \right) - \frac{1}{\mu} C^Z d\tau + (C^r J'_r + C^r) dr + C^r J'_D dD.$ 

Upon rearranging and defining

$$
M = \left(1 - \frac{1}{\mu}\right) C^{r} J'_{D} + \frac{1}{\mu} C^{Z},
$$
  

$$
R = \left(C^{r} J'_{r} + C^{r}\right),
$$

we obtain

$$
dC = (1 - \tau_{ss})M\left(dY - \frac{\alpha}{1 - \alpha}dQ - \frac{1}{1 - \tau_{ss}}d\tau\right) + Rdr.
$$

Note that  $\tau_{ss} = 0$ , so  $d\tau = dT$ , yielding

$$
dC = M\left(dY - \frac{\alpha}{1-\alpha}dQ - dT\right) + Rdr.
$$
 (31)

#### **A.1.4 Main Proof**

Linearizing goods market clearing gives

$$
dY_t = dC_{H,t} + dC_{H,t}^* + dG_t.
$$

Inserting equations (25), (26), and (28) gives

$$
dY_t = (1 - \alpha)dC_t + \eta \alpha dQ_t + \frac{\eta \alpha}{1 - \alpha} dQ_t + dG_t
$$
  
= 
$$
(1 - \alpha)dC_t + \frac{2 - \alpha}{1 - \alpha} \alpha \eta dQ_t + dG_t.
$$

Writing this in sequence space and inserting for consumption yields:

$$
dY = (1 - \alpha) \left[ M(dY - dT) - \frac{\alpha}{1 - \alpha} MdQ + Rdr \right] + \frac{2 - \alpha}{1 - \alpha} \alpha \eta dQ + dG
$$
  
=  $dG - (1 - \alpha)MdT + (1 - \alpha)Rdr + \left[ \frac{2 - \alpha}{1 - \alpha} \alpha \eta - \alpha M \right] dQ + (1 - \alpha)MdY.$ 

This is the expression from Proposition 1. Before proceeding, we find it useful to rewrite this expression by exploiting some properties of the model.

#### **A.1.5 Mapping between Income and Interest-Rate Jacobians**

We now use that  $R = - (I - M) U$  (see Lemma 1 in Auclert et al., 2021b), along with  $dQ = -U dr$  (since  $r_{ss} \rightarrow 0$ ) from the linearized real UIP condition. This allows us to rewrite the previous expression as:

$$
\begin{aligned} \left[\mathbf{I} - (1 - \alpha)\mathbf{M}\right]d\mathbf{Y} &= -(1 - \alpha)(\mathbf{I} - \mathbf{M})\mathbf{U}d\mathbf{r} - (1 - \alpha)\mathbf{M}d\mathbf{T} \\ &- \left[\frac{2 - \alpha}{1 - \alpha}\alpha\eta - \alpha\mathbf{M}\right]\mathbf{U}d\mathbf{r} + d\mathbf{G}, \end{aligned}
$$

or, after collecting terms:

$$
\left[I-(1-\alpha)M\right]dY=-\left\{(1-\alpha)I-M+\frac{2-\alpha}{1-\alpha}\alpha\eta\right\}Udr-(1-\alpha)MdT+dG.
$$

#### **A.1.6 Primary Deficits**

It is useful to state the Keynesian cross in a term related to primary deficits *dG* − *dT*. To this end, add and subtract  $(1 - \alpha)MdG$  from the previous expression, and rewrite:

$$
\begin{aligned} \left[\mathbf{I} - (1-\alpha)\mathbf{M}\right]d\mathbf{Y} &= -\left\{(1-\alpha) - \mathbf{M} + \frac{2-\alpha}{1-\alpha}\alpha\eta\right\}\mathbf{U}d\mathbf{r} \\ &+ \left[\mathbf{I} - (1-\alpha)\mathbf{M}\right]d\mathbf{G} + (1-\alpha)\mathbf{M}\left(d\mathbf{G} - d\mathbf{T}\right). \end{aligned}
$$

Upon defining  $\mathcal{G} = \left[I - (1 - \alpha)M\right]^{-1}$ , we can write this as:

$$
d\mathbf{Y} = -\mathcal{G}\left\{(1-\alpha) - \mathbf{M} + \frac{2-\alpha}{1-\alpha}\alpha\eta\right\}\mathbf{U}d\mathbf{r} + d\mathbf{G} + (1-\alpha)\mathcal{G}\mathbf{M}\left(d\mathbf{G} - d\mathbf{T}\right). \tag{32}
$$

This expression holds for a general household problem, i.e. nests both HANK and RANK. Let us now consider the RANK model. Linearize the Euler equation:

$$
dC_{t+1} = dC_t + \frac{dr_{t+1}^a}{1 + r_{ss}},
$$

using that  $\beta = (1 + r_{ss})^{-1}$  and  $C_{ss} = 1$ . Solving for  $dC_t$  and substituting recursively then gives

$$
dC_t = -\frac{1}{1 + r_{ss}} \sum_{s=1}^{\infty} dr_{t+s}^a,
$$

where we used that  $C_{\infty} = C_{ss}$  so  $dC_{\infty} = 0$ . Use  $r_{t+1}^a = r_t$  for  $t = 0, 1, ...$  and  $r_{ss} \to 0$ :

$$
dC_t = -\sum_{s=0}^{\infty} dr_{t+s}.
$$

On sequence-space form:

$$
dC=-Udr,
$$

i.e.,  $M^{RA} = 0$ , which in turn implies that  $G = I$  in the RANK model. We then obtain the following two HANK and RANK expressions directly from (32):

$$
dY^{HA} = dG - \mathcal{G}\left\{(1-\alpha) - M + \frac{2-\alpha}{1-\alpha}\alpha\eta\right\} U dr^{HA} + (1-\alpha)\mathcal{G}M(dG - dT),
$$
 (33)  

$$
dY^{RA} = dG - \left\{(1-\alpha) + \frac{2-\alpha}{1-\alpha}\alpha\eta\right\} U dr^{RA},
$$
 (34)

where we just write " $M$ " instead of " $M^{\text{HA}}$ " (and similarly for  $\mathcal{G}$ ).

### **A.2 Proof of Proposition 2**

Begin by noting that

$$
G = [I - (1 - \alpha)M]^{-1} = I + (1 - \alpha)M + (1 - \alpha)^2 M^2 + \dots
$$

Post-multiplying by  $(1 - \alpha)M$  gives

$$
(1-\alpha)\mathcal{G}M=(1-\alpha)M+(1-\alpha)^2M^2+\cdots=\mathcal{G}-I.
$$

Thus,

$$
\mathcal{G}M = -\frac{1}{1-\alpha}(I-\mathcal{G}).\tag{35}
$$

Inserting this into (32) gives

$$
dY = -\mathcal{G}\left\{(1-\alpha) - M + \frac{2-\alpha}{1-\alpha}\alpha\eta\right\} Udr + dG - (I - \mathcal{G}) (dG - dT)
$$
  
= 
$$
-\mathcal{G}\left\{(1-\alpha) - M + \frac{2-\alpha}{1-\alpha}\alpha\eta\right\} Udr + \mathcal{G}dG + (I - \mathcal{G})dT.
$$

Use now the tax rule from (9) to get that

$$
d\mathbf{Y} = -\mathcal{G}\left\{(1-\alpha)-M+\frac{2-\alpha}{1-\alpha}\alpha\eta\right\}\mathbf{U}d\mathbf{r} + \left[\mathcal{G}+\phi_G(\mathbf{I}-\mathcal{G})\right]d\mathbf{G}.
$$



Figure A.1: Decomposition of output ( $d\Upsilon$ ) when  $\alpha \rightarrow 1$  and  $\phi_{\Upsilon} = 0$ 

Note: The figure shows the decomposition of the response of output from Proposition 1 for the HANK and RANK models when  $\alpha \rightarrow 1$  and  $\phi_Y = 0$ .

Consider first the case of an active monetary policy, i.e.,  $\phi_Y > 0$ . Use the monetary policy rule in  $(10)$  to get that

$$
d\mathbf{Y} = -\mathcal{G}\left\{(1-\alpha) - \mathbf{M} + \frac{2-\alpha}{1-\alpha}\alpha\eta\right\}\mathbf{U}\phi_{Y}d\mathbf{Y} + \left[\mathcal{G} + \phi_{G}(\mathbf{I} - \mathcal{G})\right]d\mathbf{G}
$$
  
= 
$$
\left\{\mathbf{I} + \mathcal{G}\left\{(1-\alpha) - \mathbf{M} + \frac{2-\alpha}{1-\alpha}\alpha\eta\right\}\mathbf{U}\phi_{Y}\right\}^{-1}\left[\mathcal{G} + \phi_{G}(\mathbf{I} - \mathcal{G})\right]d\mathbf{G}.
$$
 (36)

When  $\alpha \to 1$ , the term in curly brackets tends to  $\infty$  (provided  $\phi_Y > 0$ ), so that its inverse converges to the null matrix, while the term in the square bracket converges to I because  $\mathcal G$  converges to I. Thus, the entire right-hand side converges to  $\mathbf 0$ , i.e.  $dY \rightarrow 0$  as  $\alpha \rightarrow 1$ . In other words, when the real rate responds ( $\phi_Y > 0$ ), there is full crowding out, such that output does not react,  $dY_t = 0$  for all *t*.

Consider now passive monetary policy, i.e.  $\phi_Y = 0$ . Insert this in (36) to get that

$$
dY=[\mathcal{G}+\phi_G(I-\mathcal{G})]dG.
$$

When  $\alpha \to 1$  it follows that  $\mathcal{G} \to 1$  by its definition, so  $d\mathbf{Y} \to d\mathbf{G}$ . In this case, there is a fiscal multiplier of 1 at all points in time,  $dY_t = dG_t$  for all *t* (see Figure A.1).

Figure A.2 shows how the multipliers of the RANK and HANK models converge as *α* increases. In the limiting case of  $\alpha \rightarrow 1$ , output converges to 0 at all points in time, i.e.  $dY_{t}^{\text{RA}} = dY_{t}^{\text{HA}} = 0$  for all *t*. More generally, it is seen that the two models feature very similar multipliers for values of *α* significantly smaller than 1, including for realistic



Figure A.2: Fiscal multipliers in HANK and RANK as a function of openness

values of *α* around 0.5.

#### **A.3 Proof of Proposition 3**

Without making any assumptions regarding government financing, we can simply use the linearized monetary policy rule—which reads  $dr = \phi_Y dY$ —directly in (33) and (34) to obtain:

$$
dY^{HA} = \Theta^{HA} \{ [I + \mathcal{G}(1-\alpha)M] \, dG - \mathcal{G}(1-\alpha)M dT \},
$$
  

$$
dY^{RA} = \Theta^{RA} dG,
$$

where

$$
\Theta^{\text{HA}} \equiv \left[ I + \mathcal{G} \left\{ (1 - \alpha) - M + \frac{2 - \alpha}{1 - \alpha} \alpha \eta \right\} U \phi_Y \right]^{-1},
$$

$$
\Theta^{\text{RA}} \equiv \left[ I + \left\{ (1 - \alpha) + \frac{2 - \alpha}{1 - \alpha} \alpha \eta \right\} U \phi_Y \right]^{-1}.
$$

In the limit  $\eta \to \infty$ , both of the matrices  $\Theta^{HA}$  and  $\Theta^{RA}$  converge to null matrices when  $\phi_Y > 0$ , so we obtain  $d\boldsymbol{Y}^{\text{RA}} = d\boldsymbol{Y}^{\text{HA}} = \boldsymbol{0}$ .

Note: The figure shows the present-value cumulative multiplier in the HANK and the RANK models (left panel), and the difference between them (right panel), as functions of the openness parameter, *α*. The figure is based on *ϕ<sup>G</sup>* = 0.1, *η* = 2, and  $\phi$ <sup>*Y*</sup> = 0.25. The cumulative fiscal multiplier is computed over 5 years, i.e. *T* = 20 in (14).

### **A.4 Proof of Proposition 4**

When we impose a balanced budget,  $dT = dG$ , (33) simplifies to

$$
d\mathbf{Y}=d\mathbf{G}-\mathcal{G}\left\{(1-\alpha)-\mathbf{M}+\frac{2-\alpha}{1-\alpha}\alpha\eta\right\}\mathbf{U}d\mathbf{r}.
$$

Comparing this expression with (34), it is seen that  $dY^{HA} = dY^{RA}$  if the matrices multiplying *dr* are equal, since *dr* is only a function of *dY*. Define these matrices as

$$
\Omega^{\text{HA}} \equiv -\mathcal{G}\left\{(1-\alpha) - M + \frac{2-\alpha}{1-\alpha}\alpha\eta\right\}U,
$$

$$
\Omega^{\text{RA}} \equiv -\left\{(1-\alpha) + \frac{2-\alpha}{1-\alpha}\alpha\eta\right\}U.
$$

Subtract the two matrices from each other to get:

$$
\Omega^{\text{RA}} - \Omega^{\text{HA}} = \left\{ (1 - \alpha) - \mathcal{G}(1 - \alpha) + \frac{2 - \alpha}{1 - \alpha} \alpha \eta - \mathcal{G} \frac{2 - \alpha}{1 - \alpha} \alpha \eta + \mathcal{G} M \right\} \mathbf{U}
$$

$$
= - \left\{ [I - \mathcal{G}] \left( 1 - \alpha + \frac{2 - \alpha}{1 - \alpha} \alpha \eta \right) + \mathcal{G} M \right\} \mathbf{U}. \tag{37}
$$

Now use the expression for  $\mathcal{G}M$  from (35) to obtain

$$
\Omega^{\text{RA}} - \Omega^{\text{HA}} = -[I - \mathcal{G}] \left( 1 - \alpha + \frac{2 - \alpha}{1 - \alpha} \alpha \eta - \frac{1}{1 - \alpha} \right) \mathbf{U}.
$$

Clearly, one way to obtain  $\mathbf{\Omega}^{\text{RA}}=\mathbf{\Omega}^{\text{HA}}$  and therefore  $d\mathbf{Y}^{\text{RA}}=d\mathbf{Y}^{\text{HA}}$  is if

$$
1-\alpha+\frac{2-\alpha}{1-\alpha}\alpha\eta-\frac{1}{1-\alpha}=0.
$$

If  $\alpha \in (0, 1)$ , the unique solution for  $\eta$  is

$$
\eta=1.
$$

This proves that  $dY^{RA} = dY^{HA}$  when  $\eta = 1$  and  $dG = dT$ . One may verify this solution simply by plugging  $\eta = 1$  into (33) and (34) to obtain

$$
dY^{RA} = dY^{HA} = dG - \frac{1}{1-\alpha}Udr.
$$

#### **A.5 Intuition behind Proposition 4**

To build intuition for the result in Proposition 4, it is useful to recall the national accounts identity for GDP, measured in units of the domestic CPI:

$$
\frac{P_{H,t}}{P_t}Y_t = C_t + \frac{P_{H,t}}{P_t}G_t + NX_t,
$$

with *NX<sup>t</sup>* defined as in Section 2. Linearizing, and writing this in sequence space:

$$
dY = dC + dG + \frac{\alpha}{1 - \alpha} dQ + dNX,
$$
\n(38)

where we have used that  $d\left(\frac{P_{H,t}}{P_t}\right)$ *Pt*  $\Big) = -\frac{\alpha}{1-\alpha} dQ_t$ . With a unitary trade elasticity, the income and substitution effects from changes in the real exchange rate exactly offset each other, and net exports remain constant,  $dNX = 0$ . The economy thus behaves almost like a closed economy: Changes in domestic real GDP comes from either private consumer demand, public spending, or movements in relative prices:

$$
dY = dC + dG + \frac{\alpha}{1-\alpha}dQ.
$$

Figure A.3 displays the contribution from each of the channels to output in the HANK and RANK model. We know from Proposition 4 that the output responses are equal in the two models. Notably, Figure A.3 shows that the contributions from each channel in (38) are also identical across the models. We can further decompose the response of consumption in the two models into contributions from labor income, *Z<sup>t</sup>* , and the real interest rate, *r<sup>t</sup>* , see Figure A.4. In the HANK model, the total consumption response is driven by both the income and intertemporal substitution effects, although the former dominates, whereas in the RANK model, the entire response is driven by intertemporal substitution. Nonetheless, the aggregate response of consumption is the same in the two models. This is effectively an application of the equivalence result for monetary policy found in Werning (2015), who showed that the aggregate effects of monetary policy in a closed economy are identical in HANK and RANK when i) the intertemporal elasticity of substitution is 1, and ii) individual income in HANK is proportional to aggregate income. Both conditions apply here. To summarize, the equivalence arises due to three different assumptions:

• The assumption of period-by-period financing implies that the multipliers in HANK and RANK would be equal in the *absence* of a monetary policy reaction in a *closed economy*, see Auclert et al. (2023).

- Given that the economy is open, active monetary policy affects the real exchange rate, and therefore net exports. The assumption of a unitary trade elasticity  $\eta = 1$  implies that net exports do not move, and the economy resembles a closed economy in this regard (see Cole and Obstfeld, 1991).
- The assumption of a unitary intertemporal elasticity of substitution then implies that we can leverage the result in Werning (2015) to obtain equivalence between HANK and RANK despite having active monetary policy.



Figure A.3: Decomposition of output using (38) with  $\eta = 1$ 

Note: The figure shows the decomposition of the response of output proposed in (38) for the HANK and RANK models when  $\eta = 1$  and the government maintains a balanced budget.



Figure A.4: Decomposition of consumption in HANK and RANK with  $\eta = 1$ 

Note: The figure shows the decomposition of the response of consumption for the HANK and RANK models when *η* = 1 and the government maintains a balanced budget.



Figure A.5: Fiscal multipliers in the stylized model

Note: The figure shows the cumulative fiscal multipliers in the HANK and RANK models in the stylized setting, i.e.  $M<sup>HA</sup>$  (left panel) and  $\widetilde{\mathcal{M}}^{RA}$  (right panel). The cumulative fiscal multipliers are computed over 5 years, i.e.  $T = 20$  in (14).

### **A.6 Multipliers in the Stylized Model**

Figure A.5 reports the cumulative fiscal multipliers underlying Figure 4 separately for the HANK and RANK models. The figure shows that the level of the fiscal multiplier in each of the two models is always moderate but non-negative.

### **B Model with Capital: Details**

This appendix provides some details regarding the version of the model extended with capital formation. In this case, domestic firms produce using Cobb-Douglas technology with labor and lagged capital as inputs:

$$
Y_t = N_t^{1-\alpha_K} K_{t-1}^{\alpha_K}.
$$

Labor is rented from households at wage rate  $w_t$ , while capital is rented from capital firms at price  $r_t^K$ . Firms optimize subject to monopolistic competition. The first-order conditions are:

$$
w_{t} = (1 - \alpha_{K}) \frac{1}{\mu} \frac{P_{H,t}}{P_{t}} \frac{Y_{t}}{N_{t}},
$$

$$
r_{t+1}^{K} = \alpha_{K} \frac{1}{\mu} \frac{P_{H,t+1}}{P_{t+1}} \frac{Y_{t+1}}{K_{t}}.
$$

Firms' (pre-tax) profits are then given by

$$
D_t^f = \frac{P_{H,t}}{P_t} Y_t - w_t N_t - r_t^K K_{t-1} - F.
$$

Capital firms invest and rent capital to final goods firms. Their profits are given by

$$
D_t^k = r_t^K K_{t-1} - I_t - F_k,
$$

where  $F_k$  is a fixed cost set to ensure that profits are zero for the capital firms in steady state. Capital firms maximize the discounted sum of profits facing a virtual adjustment cost of

$$
f\left(\frac{I_t}{I_{t-1}}\right) = \frac{\phi^I}{2}\left(\frac{I_t}{I_{t-1}} - 1\right)^2,
$$

subject to the law of motion for capital

$$
K_t = \left(1 - \delta^K\right)K_{t-1} + I_t.
$$

Denoting by  $Q_t^I$  the Lagrange multiplier on the capital accumulation constraint, the

Lagrangian can be stated as:

$$
\mathcal{L} = \sum_{t=0}^{\infty} d_t \left\{ \left[ r_t^K K_{t-1} - I_t - f(I_t/I_{t-1}) I_t \right] - Q_t^I \left\{ K_t - \left( 1 - \delta^K \right) K_{t-1} - I_t \right\} \right\},
$$

where

$$
d_t \equiv (1 + r_0)^{-1} \dots (1 + r_{t-1}), \text{ for } t = 1, 2, \dots
$$
  

$$
d_0 \equiv 1,
$$

is the discount factor. The derivative w.r.t. investment is

$$
\frac{\partial \mathcal{L}}{\partial I_t} = -d_t - d_t \frac{\partial f_t}{\partial I_t} I_t - d_t f_t + d_t Q_t^I - d_{t+1} \frac{\partial f_{t+1}}{\partial I_t} I_{t+1},
$$
\n
$$
= -d_t - d_t \phi^I \left( \frac{I_t}{I_{t-1}} - 1 \right) \frac{I_t}{I_{t-1}} - d_t \frac{\phi^I}{2} \left( \frac{I_t}{I_{t-1}} - 1 \right)^2
$$
\n
$$
+ d_t Q_t^I + d_{t+1} \phi^I \left( \frac{I_{t+1}}{I_t} - 1 \right) \left( \frac{I_{t+1}}{I_t} \right)^2,
$$

where we have defined the short-hand  $f_t \equiv f(I_t/I_{t-1})$ , and we have used that

$$
\frac{\partial f_t}{\partial I_t} = \phi^I \left( \frac{I_t}{I_{t-1}} - 1 \right) \frac{1}{I_{t-1}},
$$

$$
\frac{\partial f_{t+1}}{\partial I_t} = -\phi^I \left( \frac{I_{t+1}}{I_t} - 1 \right) \left( \frac{I_{t+1}}{I_t} \right)^2.
$$

Setting this equal to zero and dividing by −*d<sup>t</sup>* yields

$$
0 = 1 + \phi^I \left( \frac{I_t}{I_{t-1}} - 1 \right) \frac{I_t}{I_{t-1}} + \frac{\phi^I}{2} \left( \frac{I_t}{I_{t-1}} - 1 \right)^2 - Q_t^I - \frac{1}{1 + r_t} \phi^I \left( \frac{I_{t+1}}{I_t} - 1 \right) \left( \frac{I_{t+1}}{I_t} \right)^2.
$$

Rearrange to get:

$$
1 + \phi^I \left( \frac{I_t}{I_{t-1}} - 1 \right) \frac{I_t}{I_{t-1}} + \frac{\phi^I}{2} \left( \frac{I_t}{I_{t-1}} - 1 \right)^2
$$
  
=  $Q_t^I + \frac{1}{1 + r_t} \phi^I \left( \frac{I_{t+1}}{I_t} - 1 \right) \left( \frac{I_{t+1}}{I_t} \right)^2$ .

The derivative w.r.t. capital is:

$$
\frac{\partial \mathcal{L}}{\partial K_t} = d_{t+1} r_{t+1}^K - d_t Q_t^I + d_{t+1} (1 + \delta^K) Q_{t+1}^I.
$$

Set this to zero and divide by *d<sup>t</sup>* :

$$
Q_t^I = \frac{1}{1+r_t} \left[ (1-\delta^K) Q_{t+1}^I + r_{t+1}^K \right].
$$

In steady state, the first FOC implies that

$$
Q_{ss}^I=1.
$$

The second FOC then implies that

$$
r_{ss}^K = r_{ss} + \delta^K.
$$

We assume that overall capital is a CES good assembled from domestic capital goods (owned by domestic firms) and imported capital goods using CES technology identical to the one used by households. With a dynamic elasticity of substitution this gives:

$$
I_{F,t} = \omega_I \left( \hat{p}_{F,t}^I \right)^{-\eta} I_t, \quad \hat{p}_{F,t}^I = \left( \hat{p}_{F,t-1}^I \right)^{\rho_{\eta}} \left( \frac{P_{F,t}^I}{P_t^I} \right)^{1-\rho_{\eta}},
$$
  

$$
I_{H,t} = (1 - \omega_I) \left( \hat{p}_{H,t}^I \right)^{-\eta} I_t, \quad \hat{p}_{H,t}^I = \left( \hat{p}_{H,t-1}^I \right)^{\rho_{\eta}} \left( \frac{P_{H,t}^I}{P_t^I} \right)^{1-\rho_{\eta}},
$$

where  $\omega_I$  is the steady-state share of investment goods imported from abroad. We assume that the price of imported final goods and investment goods are equal such that  $P_{F,t}^I = P_{F,t}$ . The price of domestic investment goods is simply  $P_{H,t}^I = P_{H,t}$ . Goods market clearing is

$$
Y_t = C_{H,t} + C_{H,t}^* + G_t + I_{H,t} + \frac{P_t}{P_{H,t}}F + \frac{P_t}{P_{H,t}}F_k.
$$

The adjustment cost does not appear here, as it is virtual. For the calibration, we set a standard capital share of  $\alpha_K = 0.33$ , while we set  $\delta^K = 0.05/4$  and  $\phi^I = 9.6$  following Auclert et al. (2020). We assume that the import share of investment goods equals the import of share of final goods,  $\omega_I = \alpha$ , since investment goods display a high

import content empirically, see e.g. Christiano et al. (2011), who report an import content in Sweden of roughly 43%. We calibrate the level of these import shares to match the same overall level of imports to GDP as in the baseline model. This gives  $\omega_I = \alpha = 0.68$ .